

Subprograms

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May 16, 2019

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- 2 Evaluation strategy (Argument Passing)
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Subprograms

- At the origin, snippets copied and pasted from other sources
 - ▶ Impact on memory management;
 - ▶ Impact on separated compilation;
 - ▶ Modular programming: first level of interface/abstraction.
- First impact on Software Engineering: “top-down” conception, by refinements.
- Generalizations: modules and/or objects.

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Procedures vs. Functions

Procedure Subprograms with no return value.

Procedures have side effects

Function Subprograms that return something.

(Pure) Functions do not have side effects

Ada, Pascal, ... have two reserved keywords **procedure** and **function**
BUT function generally describe subprograms with return values,
while procedures do not return values

Distinction sometimes blurred by the language:
(e.g., using void ALGOL, C, Tiger...).

Procedures vs. Functions

```
Function Add(A, B : Integer) : Integer;  
Begin  
  Add := A + B;  
End;
```

Functions in Pascal

```
Procedure finish(name: String);  
Begin  
  WriteLn('Goodbye_', name);  
End;
```

Procedures in Pascal

Vocabulary

Formal Argument Arguments of a subprogram declaration.

```
let function
  sum (x: int, y: int): int = x + y
```

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let function  
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```

Effective Argument Arguments of a call to a subprogram.

```
sum (40, 12)
```


Vocabulary

Formal Argument Arguments of a subprogram declaration.

```
let function  
    sum (x: int, y: int): int = x + y
```

Effective Argument Arguments of a call to a subprogram.

```
sum (40, 12)
```

Parameter Please reserve it for templates.

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Functions: Side effects

Using functions with side effects is very dangerous. For instance:

```
foo =getc () +getc () *getc ();
```

is undefined (\neq nondeterministic). *On purpose!*

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Default arguments

```
int sum(int a, int b = 21, int c = 42,  
        int d = 42){  
    return a + b + c + d;  
}
```

Default Arguments in C++

- `sum(1, 2, 3, 4)` is fine
- `sum(1, 2)` is also fine
- But what if we want to call `sum (b = 1, a = 2)` with `c`'s and `d`'s default value?

Named Argument (Some sugar)

In Ada, named arguments and/or default values:

```
put (number      : in float;  
     before      : in integer := 2;  
     after       : in integer := 2;  
     exponent    : in integer := 2) ...
```

Some Ada function declaration

```
put (pi, 1, 2, 3);  
put (pi, 1);  
put (pi, 2, 2, 4);  
put (pi, before => 2,  
     after => 2, exponent => 4);  
put (pi, exponent => 4);
```

Possible invocations

Named Arguments

Named parameters are available in many languages: Perl, Python, C#, Fortran95, Go, Haskell, Lua, Ocaml, Lisp, Scala, Swift/ObjectiveC (**fixed order of named parameters!**), ...

- No need to remember the order of parameters
- No need to guess specific **default's** values
- More Flexible
- Clarity

Simulate Named Argument

Can we simulate **named arguments** in C++ or Java?

Yes : **Named parameter idiom** uses a proxy object for passing the parameters.

Named Parameter Idiom 1/2

```
class foo_param{
private:
    int a = 0, b = 0;
    foo_param() = default; // make it private
public:
    foo_param& with_a(int provided){
        a = provided; return *this;
    }
    foo_param& with_b(int provided){
        b = provided; return *this;
    }
    static foo_param create(){
        return foo_param();
    }
};
```

Named Parameter Idiom 2/2

```
void foo(foo_param& f)
{
    // ...
}

foo(foo_param::create().with_b(1)
    .with_a(2));
```

Named Parameter Idiom 2/2

```
void foo(foo_param& f)
{
    // ...
}

foo(foo_param::create().with_b(1)
    .with_a(2));
```

Works ... but require one specific class per function

For C++, Boost::Parameter library also offer a generic implementation

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Argument passing

From a naive point of view (and for **strict evaluation**), three possible modes: **in**, **out**, **in-out**. But there are different flavors.

	Val	ValConst	RefConst	Res	Ref	ValRes	Name
ALGOL 60	*						*
Fortran					?	?	
PL/1					?	?	
ALGOL 68		*			*		
Pascal	*				*		
C	*	?			?		
Modula 2	*				?		
Ada (simple types)		*		*		*	
Ada (others)		?	?	?	?	?	
Alphard		*	*		*		

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- Call by Name
- Call by Need
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Call by Value – definition

Passing arguments to a function copies the actual value of an argument into the formal parameter of the function.

In this case, changes made to the parameter inside the function have no effect on the argument.

```
def foo(val):  
    val = 1  
  
i = 12  
print (i)
```

Call by value in Python – **output: 12**

Pros & Cons

- **Safer:** variables cannot be accidentally modified
- **Copy:** variables are copied into formal parameter *even for huge data*
- **Evaluation before call:** resolution of formal parameters must be done before a call
 - ▶ Left-to-right: Java, Common Lisp, Eiffel, C#, Forth
 - ▶ Right-to-left: Caml, Pascal
 - ▶ Unspecified: C, C++, Delphi, , Ruby

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Call by Reference – definition

Passing arguments to a function copies the actual address of an argument into the formal parameter of the function.

In this case, changes made to the parameter inside the function will have effect on the argument.

```
void swap(int &x, int &y)
    { int aux = x; x = y; y = aux; }

int main() {
    int x = 2, y = 3;
    swap(a, b);
    printf("%d, □%d\n", x, y);
}
```

Call by reference in C++ – **output: 3 2**

Pros & Cons

- **Faster** than call-by-value if data structure have a large size.
- **Readability & Undesirable behavior:** a special attention may be considered when doing operations on multiple references **since they can all refer to the same object**

```
void xor_swap(int &x, int &y) {  
    x = x ^ y;  
    y = x ^ y;  
    x = x ^ y;  
}
```

Call by reference in C++ may lead to undesirable behavior when x and y refers the same object (zeroing x and y)

Notes on call-by-reference

- *swap(foo, foo)* is forbidden in Pascal but what about *swap(foo[bar], foo[baz])* ...

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Call by Value-Result – definition

Passing arguments to a function copies the argument into the formal parameter of the function.

The values are then copied back when exiting the function

In this case, changes made to the parameter inside the function will only reflect on the argument at the end of the function.

Call by Value-Result – Example

```
procedure Tryit is
  procedure swap (i1, i2: in out integer) is
    tmp: integer;
  begin
    tmp := i1;    i1 := i2;    i2 := tmp;
  end swap;

  a : integer := 1;    b : integer := 2;
begin
  swap(a, b);
  Put_Line(Integer'Image (a) & "␣" &
           Integer'Image (b)) ;
end Tryit;
```

Call by Value-result in Ada – **output: 2 1**

Notes on call-by-value-result

Pros & Cons

- **Safety** other thread will only see consistent values since changes made will not show up until after the end of the function.
- **Local copies:** but they can be sometimes avoided by the compiler

Notes on call-by-value-result

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Notes on call-by-value-result

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- **Safety** other thread will only see consistent values since changes made will not show up until after the end of the function.
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Remarks:

- Also called: **Call by copy-restore, Call by copy-in copy-out**

Notes on call-by-value-result

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- **Local copies:** but they can be sometimes avoided by the compiler

Remarks:

- Also called: **Call by copy-restore**, **Call by copy-in copy-out**
- If the reference is passed to the callee uninitialized, this evaluation strategy is called **call by result**.

Notes on call-by-value-result

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- Used in multiprocessing contexts.

Notes on call-by-value-result

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Remarks:

- Also called: **Call by copy-restore**, **Call by copy-in copy-out**
- If the reference is passed to the callee uninitialized, this evaluation strategy is called **call by result**.
- Used in multiprocessing contexts.
- Multiple interpretations:
 - ▶ Ada: Evaluates arguments once, during function call
 - ▶ AlgolW: Evaluates arguments during call **AND** when exiting the function

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An outsider: call by name

(In ALGOL 60) It behaves as a macro would, including with name captures: the argument is evaluated *at each use*.

- Try to write some code which results in a completely different result had SWAP been a function.

```
#define SWAP (Foo , Bar) \  
do {                      \  
    int tmp_ = (Foo);     \  
    (Foo) = (Bar);        \  
    (Bar) = tmp_;         \  
} while (0)
```

- In ALGOL 60, a *compiled* language, “thunks” were introduced: snippets of code that return the l-value when evaluated.

An application of call by name: Jensen's Device

- General computation of a sum of a series $\sum_{k=l}^u a_k$:

```
real procedure Sum(k, l, u, ak)
  value l, u;
  integer k, l, u;
  real ak;
  comment 'k' and 'ak' are passed by name;
begin
  real s;
  s := 0;
  for k := l step 1 until u do
    s := s + ak;
  Sum := s
end;
```

- Computing the first 100 terms of a real array V[]:

```
Sum(i, 1, 100, V[i])
```


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Call by Need

Call by need is a memoized variant of call by name where, if the function argument is evaluated, that value is stored for subsequent uses.

The argument is then evaluated only once, during its first use.

What if $y = 0$ in the following code?

```
let function loop (z: int):int =
    if z > 0 then z else loop (z)
    function f      (x: int):int =
        if y > 8 then x else -y
in
    /* ≡ 'if y > 8 then loop (y) else -y' ? */
    f (loop (y))
end
```

Call by name

Don't pass the evaluation of the expression, but a “thunk” computing it:

```
let var      a      := 5 + 7 in
    a + 10
end
==> let function a () := 5 + 7 in
    a () + 10
end
```

Call by need

The thunk is evaluated once and only once. Add a “memo” field.

Lazy evaluation 1

```
easydiff f x h = (f (x + h) - f (x)) / h

repeat f a = a : repeat f (f a)
halve x = x / 2
differentiate h0 f x = map (easydiff f x) (repeat halve

within eps (a : b : rest)
  | abs (b - a) <= eps = b
  | otherwise          = within eps (b : rest)

relative eps (a : b : rest)) =
  | abs (b - a) <= eps * abs b = b
  | otherwise                  = relative eps (b : rest)
within eps (differentiate h0 f x)
```

Slow convergence... Suppose the existence of an error term:

```
a (i)      = A + B * (2 ** n) * (h ** n)
a (i + 1) = A + B * (h ** n)
```

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Exhibit the differences (Explicit lyrics...)

```
var t    : integer
    foo: array [1..2] of integer;

procedure shoot_my (x : Mode integer);
begin
    foo[1] := 6;
    t      := 2;
    x      := x + 3;
end;

begin
    foo[1] := 1;
    foo[2] := 2;
    t      := 1;
    shoot_my (foo[t]);
end.
```

Exhibit the differences (Explicit lyrics...)

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    x      := x + 3;
end;

begin
    foo[1] := 1;
    foo[2] := 2;
    t      := 1;
    shoot_my (foo[t]);
end.
```



<i>Mode</i>	foo[1]	foo[2]	t
Val			

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end;

begin
    foo[1] := 1;
    foo[2] := 2;
    t      := 1;
    shoot_my (foo[t]);
end.
```



<i>Mode</i>	foo[1]	foo[2]	t
Val	6	2	2

Val-Res (ALGOL W)

Exhibit the differences (Explicit lyrics...)

```
var t : integer
    foo: array [1..2] of integer;

procedure shoot_my (x : Mode integer);
begin
    foo[1] := 6;
    t      := 2;
    x      := x + 3;
end;

begin
    foo[1] := 1;
    foo[2] := 2;
    t      := 1;
    shoot_my (foo[t]);
end.
```



<i>Mode</i>	foo[1]	foo[2]	t
Val	6	2	2
Val-Res (ALGOL W)	6	4	2
Val-Res (Ada)			

Exhibit the differences (Explicit lyrics...)

```
var t : integer
    foo: array [1..2] of integer;

procedure shoot_my (x : Mode integer);
begin
    foo[1] := 6;
    t      := 2;
    x      := x + 3;
end;

begin
    foo[1] := 1;
    foo[2] := 2;
    t      := 1;
    shoot_my (foo[t]);
end.
```



<i>Mode</i>	foo[1]	foo[2]	t
Val	6	2	2
Val-Res (ALGOL W)	6	4	2
Val-Res (Ada)	4	2	2
Ref			

Exhibit the differences (Explicit lyrics...)

```
var t : integer
    foo: array [1..2] of integer;

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    foo[1] := 6;
    t      := 2;
    x      := x + 3;
end;

begin
    foo[1] := 1;
    foo[2] := 2;
    t      := 1;
    shoot_my (foo[t]);
end.
```



<i>Mode</i>	foo[1]	foo[2]	t
Val	6	2	2
Val-Res (ALGOL W)	6	4	2
Val-Res (Ada)	4	2	2
Ref	9	2	2
Name			

Exhibit the differences (Explicit lyrics...)

```
var t : integer
    foo: array [1..2] of integer;

procedure shoot_my (x : Mode integer);
begin
    foo[1] := 6;
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    x      := x + 3;
end;

begin
    foo[1] := 1;
    foo[2] := 2;
    t      := 1;
    shoot_my (foo[t]);
end.
```



<i>Mode</i>	foo[1]	foo[2]	t
Val	6	2	2
Val-Res (ALGOL W)	6	4	2
Val-Res (Ada)	4	2	2
Ref	9	2	2
Name	6	5	2

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Call by Sharing – definition

Call by sharing implies that values in the language are based on objects rather than primitive types, i.e. that all values are "boxed"

Differs from both call-by-value and call-by-reference.

```
def f(list):  
    list.append(1)
```

```
m = []  
f(m)  
print(m)
```

Call by sharing in Python –
output: [1]

```
def f(list):  
    list = [1]
```

```
m = []  
f(m)  
print(m)
```

Call by sharing in Python –
output: []

Notes on Call-by-sharing

Mutations of arguments performed by the called routine will be visible to the caller.

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Access is not given to the variables of the caller, but merely to certain objects

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Can be seen as "call by value" in the case where the value is an object reference

Notes on Call-by-sharing

Mutations of arguments performed by the called routine will be visible to the caller.

Access is not given to the variables of the caller, but merely to certain objects

Can be seen as "call by value" in the case where the value is an object reference

- First introduced by Barbara Liskov for CLU language (1974)
- Widely used by: Python, Java, Ruby, JavaScript, Scheme, OCaml, AppleScript, ...
- **call by sharing** is not in common use; the terminology is inconsistent across different sources.

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Return Statement

What is the purpose of the return statement?

Is there a best way to return something?

Is there a best way to return something?

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 - return via dedicated keyword
 - return via function's name
 - return via specific variable
 - return the last computed value
 - named return values
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Return via a dedicated keyword 1/2

```
int compute(int a, int b) {  
    int res = a+b;  
    // Some computation  
    return res;  
}
```

C's return statement uses the **return** keyword

```
int compute(int a, int b) {  
    int r_val = a+b;  
    // Some computation  
    return r_val;  
}
```

Java's return statement also uses the **return** keyword

Return via a dedicated keyword 2/2

The **return** statement breaks the current fonction (also for C++, Java, Ada, Modula2).

- Clarity
- Complexify the code
 - ▶ No naming convention
 - ▶ No homogeneous return inside a given fonction
 - ▶ Blur the comprehension via initialisation, intermediate computation, ...

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Return via function's name

```
function sum (a, b: integer): integer;  
begin  
    sum := a + b;  
end;
```

Pascal's return statement uses the name of the function

Return via function's name

```
function sum (a, b: integer): integer;  
begin  
    sum := a + b;  
end;
```

Pascal's return statement uses the name of the function

The name of the function is treated as a variable name (also for Fortran, ALGOL, ALGOL68, Simula)

- The “return” may not be the latest statement
- **Ambiguous**
 - ▶ For recursion **sum** denotes a variable **AND** a function
 - ▶ Is *somevar := sum* legal? (Yes for Pascal, No for Fortan)

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Return via a specific variable (1/2)

```
always_true : BOOLEAN
do
  Result := true
end
```

```
always_one : INTEGER
do
  Result := 1
end
```

```
always_bar : STRING
do
  Result := "bar"
end
```

Effail's return statement uses the keyword **Result**

Return via a specific variable (2/2)

- The value returned by a function is whatever value is in **Result** when the function ends.
- The return value of a feature is set by assigning it to the **Result** variable (initialised automatically to a default value).
- Unlike other languages, the **return** statement does not exist.

Only in Eiffel (to my knowledge)

- Clarity
- Ambiguous if the language support nested functions

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Return the last computed value 1 / 2

```
(defun double (x) (* x 2))
```

Lisp's return value is the last computed value

```
fn is_divisible_by(lhs: u32, rhs: u32) -> bool {  
    if rhs == 0 {  
        return false;  
    }  
    // The 'return' keyword isn't necessary  
    lhs % rhs == 0  
}
```

For expressions, **Rust's return value** is the last computed value

Return the last computed value 2 / 2

In **expression-oriented programming language** (also Lisp, Perl, Javascript and Ruby) the return statement can be omitted.

- **Instead that the last evaluated expression is the return value.**
- A "last expression" is mandatory in Rust
- If no "return" Python returns **None** and Javascript **undefined**

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 - return via specific variable
 - return the last computed value
 - **named return values**
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Named return values and Naked return

```
func make(r int, i int) (re int, im int) {  
    re = r  
    im = i  
    return  
}
```

Go combines Named returns values and naked return

Named return values and Naked return

```
func make(r int, i int) (re int, im int) {  
    re = r  
    im = i  
    return  
}
```

Go combines Named returns values and naked return

- No declaration/initialisation in the body of the function
- It serves as documentation.
- Functions that return multiple values are hard to name clearly
GetUsernameAndPassword
- The signature of the function is slightly more difficult to read

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Subprograms as arguments

```
function diff (f(x: real): real,  
              x, h: real) : real;  
begin  
  if h = 0 then  
    slope := 0  
  else  
    slope := (f (x + h) - f (x)) / h;  
    diff := slope  
  end  
  
begin  
  ...  
  diff (sin, 1, 0.01);  
  ...  
end
```

- Typing difficulties ignored in ALGOL 60, Fortran, original Pascal and C: the function-argument was not typed.
- Today function types are available in most languages (except in some OOL).
- Doesn't exist in Ada. Simulated by a function parametrized routine. But you have to instantiate...

Anonymous subprograms

In all the functional languages, but not only (see automake)...

```
use Getopt::Long;
Getopt::Long::config ("bundling", "pass_through");
Getopt::Long::GetOptions
(
    'version'           => &version,
    'help'              => &usage,
    'libdir:s'          => $libdir,
    'gnu'               => sub { set_strictness ('gnu'); },
    'gnits'             => sub { set_strictness ('gnits'); },
    'cygnus'           => $cygnus_mode,
    'foreign'          => sub { set_strictness ('foreign'); },
    'include-deps'     => sub { $use_dependencies = 1; },
    'ignore-deps'     => sub { $use_dependencies = 0; },
    'no-force'         => sub { $force_generation = 0; },
    'o|output-dir:s'  => $output_directory,
    'v|verbose'        => $verbose,
)
or exit 1;
```

Environment capture

Functional languages with block structure.

```
let type intfun = int -> int
    function add (n: int) : intfun =
        let function res (m: int): int = n + m in
        var addFive : intfun := add (5)
        var addTen   := add (10)
        var twenty   := addTen (addFive (5))
in
    twenty = 20
end
```

Create *closures*: a pointer to the (runtime) environment in addition to a pointer to the code. Somewhat hard to implement [Chap. 15](appel.98.modern).

